- **1.** (i) {2}
- (ii)  $\{0, 1\}$
- (iii)  $\{1, p\}$

- 2. (i)  $\{0, -1, 1\}$
- (ii)  $\frac{-11}{3}$
- (iii)  $\left\{-\sqrt{3}, -\sqrt{2}, \sqrt{2}, \sqrt{3}\right\}$

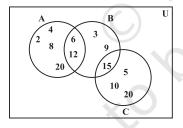
- 3.  $\{1, 2, 2^2, 2^3, \dots 2^{p-1}, (2^p-1)\}$
- **4.** (i) True
- (ii) False
- (iii) True

- **7.** (i) {2, 4, 6, 8, ..., 98} (ii) (1,4, 9, 16, 25, 36, 49, 64, 81,}
- **8.** (i) {4, 8, 12} (ii) {7, 8, 9}
- (iii)  $\frac{1}{2}$ , 1,  $\frac{3}{2}$  (iv)  $\{0, 1, 2\}$

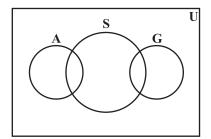
- **9.** (i) {4, 5, 6, ....10}
- (ii) {5}

(iii)  $\{1, 2, 3, 4, 5\}$ 

**10.** 



11.



- **13.** True
- 14. False
- **15.** True

- **16.** True
- **17.** True
- **22.**  $T = \{10\}$
- (i) 2 (ii) 3 (iii) 3 (iv) 9 24.
- 25. 25
- **26.** 20
- **27.** (a) 3300 (b) 4000

- 28.
  - (i) 6, (ii) 3, (iii) 9, (iv) 1, (v) 2, (vi) 6, (vii) 30, (viii) 20 29. C
    - **32.** D
- **33.** C

34. D

**30.** 

- **31.** B **35.** B
- **36.** B
- **37.** C

39. C 38.  $\mathbf{C}$ **40.** A **41.** B **43.** C **44.** [1,2] **42.** В **45.** 1 46. 47.  $A \cap B'$ **48.** {\phi, {1}, {2}, {1, 2} n (B)  $\{0, 1, 2, 3, 4, 5, 6, 8\}$  **50.**(i)  $\{1, 5, 9, 10\}$  (ii)  $\{1, 2, 3, 5, 6, 7, 9, 10\}$ 49. **51.** 

51.  $A \cup B'$  52. (i)  $\leftrightarrow$  (b) (ii)  $\leftrightarrow$  (c) (iii)  $\leftrightarrow$  (a) (iv)  $\leftrightarrow$  (f) (v)  $\leftrightarrow$  (d) (vi)  $\leftrightarrow$  (e) 53. True 54. False 55. False 56. True

**57.** True **58.** False

## 2.3 EXERCISE

**1.** (i) {(-1,1), (-1,3), (2,1), (2,3), (3,1), (3,3)}

(ii) 
$$\{(1,-1), (1,2), (1,3), (3,-1), (3,2), (3,3)\}$$

(iii)  $\{(1, 1), (1, 3), (3, 1), (3, 3)\}$ 

(iv) 
$$\{(-1,-1),(-1,2),(-1,3),(2,-1),(2,2),(2,3),(3,-1),(3,2),(3,3)\}$$

**2.** {(0, 1), (0, 2), (1, 1), (1, 2), (2, 1), (2, 2)}

3. (i)  $\{(0,3),(1,3)\}$ 

(ii) 
$$\{(0,2), (0,3), (0,4), (0,5), (1,2), (1,3), (1,4), (1,5)\}$$

4. (i)  $a = \frac{11}{3}$  and  $b = \frac{2}{3}$  (ii) a = 0 and b = -2

**5.** (i) {(1, 4), (2, 3), (3, 2), (4, 1)}

(ii) 
$$\{(1,1),(1,2),(1,3),(2,1),(2,2),(3,1)\}$$

(iii)  $\{(4,5),(5,4),(5,5)\}$ 

**6.** Domain of  $R = \{0, 3, 4, 5\} = Range of R$ 

7. Domain of  $R_1 = [-5, 5]$  and Range of  $R_1 = [-3, 17]$ 

8.  $R_2 = \{(0, 8), (8, 0), (0, -8), (-8, 0)\}$ 

9. Domain of  $R_3 = \mathbf{R}$  and range of  $R_3 = \mathbf{R}^+ \cup \{0\}$ 

10. (i) h is not a function (ii) f is a function (iii) g is a function (iv) s is a function(v) t is a constant function

11. (a) 6 (b)  $\frac{1364}{4}$  (c) 13 (d)  $t^2-4$  (e) t+5

**12.** (a) x = 4 (b) x > 4

**13.** (i)  $(f+g) x = x^2 + 2x + 2$  (ii)  $(f-g) x = 2x - x^2$ 

(iii) 
$$(fg) x = 2x^3 + x^3 + 2x + 1$$
 (iv)  $\left(\frac{f}{g}\right) x = \frac{2x+1}{x^2+1}$ 

**14.** (i) 
$$f = \{(-1, 0), (0, 1), (3, 28), (7, 344), (9, 730)\}$$

**15.** 
$$x = -1$$
,  $\frac{4}{3}$ 

**16.** Yes, 
$$\alpha = 2$$
,  $\beta = -1$ 

17. (i) 
$$R - \{2n\pi : n \in Z\}$$

(ii) R<sup>+</sup>

(iii) R

$$(iv)R - \{-1, 1\}$$

(v) 
$$R - \{4\}$$

18. (i) 
$$[\frac{3}{2}, \infty)$$

(iii) 
$$[0, \infty)$$

(iv) 
$$[-2, 4]$$

$$-2x, -3 \le x < -2$$

19. 
$$f(x) = 4$$
,  $-2 \le x < 2$   
2.  $2 \le x \le 3$ 

**21.** (i) 
$$(f+g) x = \sqrt{x} + x$$

(ii) 
$$(f-g) x = \sqrt{x} - x$$

(iii) 
$$(fg) x = \frac{3}{x^2}$$

(iv) 
$$\left(\frac{f}{g}\right)x = \frac{1}{\sqrt{x}}$$

- 22. Domain of  $f = (5, \infty)$  and Range of  $f = R^+$
- **24.** D
- **25.** D
- **26.** B
- **27.** C

- **28.** B
- **29.** B
- **30.** A
- **31.** C

- **32.** C
- **33.** A
- **34.** B
- 35. A

- **36.** {2, 3, 4, 5}
- 37. (a)  $\leftrightarrow$  (iii) (b)  $\leftrightarrow$  (iv) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (i)

- 38. False
- **39.** False
- **40.** True
- **41.** False

**42.** True.

4. 
$$\frac{56}{33}$$

$$5. \ \frac{2\cos x}{\sqrt{\cos 2x}}$$

8. 
$$\frac{1}{\sqrt{2}+1}$$

**15.** 
$$\theta = n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{4}$$

$$16. \quad \theta = 2n\pi + \frac{7\pi}{4}$$

17. 
$$\theta = 2n\pi \pm \frac{\pi}{3}$$

**18.** 
$$\theta = \frac{\pi}{3}, \frac{5\pi}{3}$$

19. 
$$x = \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{2}$$

25. 
$$\frac{23}{17}$$
  $\frac{\sqrt{3}-1}{2} + \frac{1}{\sqrt{2}}$ 

26. 
$$\frac{3}{2}$$

**27.** 
$$n\pi \pm \frac{\pi}{4}$$

28. 
$$\frac{n\pi}{2} \pm \frac{\pi}{8}$$

**29.** 
$$\theta = 2n\pi \pm \frac{\pi}{4} + \frac{\pi}{12}$$

**63.** 
$$\frac{1}{4} [4 - 3(a^2 - 1)^2], \sqrt{2 - a^2}$$

**64.** 
$$x^2 - \frac{2}{\sin 2A}x + 1$$
 **65.** 13

**76.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (iii)

1. 
$$P(n) : 2n < \angle n$$

**2.** 
$$P(n): 1 + 2 + 3 + ... + n = \frac{n(n+1)}{2}$$

$$2. -1 + i$$

**2.** 
$$-1 + i$$
 **3.**  $(0, -2)$ 

4. 
$$\frac{2}{5}$$

6. 
$$i\cot \frac{\theta}{2}$$

(1,0) 6. 
$$i\cot \frac{\theta}{2}$$
 11.  $\frac{3}{2}-2i$ 

12. 
$$\frac{1}{2}$$
 - 2

14. 
$$\frac{10}{3}$$
, 0,  $\frac{2}{3}$  15. 1

**21.** 
$$\sqrt{2} \pm i\sqrt{2}, -\sqrt{2} \pm i\sqrt{2}$$

**22.** 
$$-2-i$$

23. 
$$\sqrt{2} \cos \frac{5\pi}{12} + i \sin \frac{5\pi}{12}$$

**25.** (i) 
$$(a^2 + b^2)(|z_1|^2 + |z_2|^2)$$

(iii) 
$$-2$$
 (iv) 0 (v)  $\frac{1}{2} - \frac{i}{2}$ 

(vi) 
$$\overline{z}_1$$
 (vii) 0

$$(x) - 2\sqrt{3} + 2i$$

**27.** (a) 
$$\leftrightarrow$$
 (v),

(b) 
$$\leftrightarrow$$
 (iii),

(c) 
$$\leftrightarrow$$
 (i),

$$(d) \leftrightarrow (iv),$$

(e) 
$$\leftrightarrow$$
 (ii),

$$(c) \leftrightarrow (i),$$
  
 $(f) \leftrightarrow (vi),$ 

$$(g) \leftrightarrow (viii)$$
 and

(h) 
$$\leftrightarrow$$
 (vii)

28. 
$$\frac{-2}{25} - i\frac{11}{25}$$

$$30. \frac{(a^2+1)^4}{4a^2+1}$$

**30.** 
$$\frac{(a^2+1)^4}{4a^2+1}$$
 **31.**  $-2\sqrt{3}+2i$ 

33. 
$$\frac{2\pi}{3}$$

1. 
$$\frac{1}{3} \le x \le 1$$

1. 
$$\frac{1}{3} \le x \le 1$$
 2.  $[0,1] \cup [3,4]$  3.  $(-\infty, -5) \cup (-3, 3) \cup [5, \infty)$ 

4. 
$$[-4,-2] \cup [2,6]$$
 5.  $\frac{-34}{3},\frac{22}{3}$ 

- More than 2000. 7.
- 8. Between 7.77 and 8.77.
- More than 230 litres but less than 920 litres. 9.
- 10. Between 104 °F and 113 °F
- **11.** 41 cm.
- 12. Between 8 km and 10 km
- 13. No Solution

**14.** 
$$x + y \le 20$$
,  $3x + 2y \le 48$ ,  $x \ge 0$ ,  $y \ge 0$ 

**15.** 
$$x + y \le 8$$
,  $x + y \ge 4$ ,  $x \le 5$ ,  $y \le 5$ ,  $x \ge 0$ ,  $y \ge 0$ 

- 17. No Solution.
- **19.** C
- **20.** C
- **21.** A
- **22.** B

- **23.** D
- 24. C
- **25.** B
- **26.** A

- **27.** D
- **28.** B
- **29.** A
- **30.** B

- **31.** (i) F
- (ii) F
- (iii) T
- (iv) F

- (v) T
- (vi) F
- (vii) T
- (viii) F

```
(ix) T
                          (x) F
                                                      (xi) T
                                                                              (xii) F
                         (xiv) T
      (xiii)F
                                                      (xv) T.
32. (i) ≤
                                                      (iii) >
                                                                              (iv) >
                           (ii) \geq
      (v) >
                           (vi) >
                                                      (vii) < , >
                                                                              (viii) \leq .
                                         7.3 EXERCISE
1.
      1440
                           2. 481
                                                        3. 780
                                                                                 4. 144
5.
                            6. 3960
                                                       7. 4,68000
                                                                                8. 200
      22
       ^{n-3}C_{r-3}(r-2)!3! 10. 14400
                                                       11. 112
                                                                               15. r = 3
16. 192
                                                      18. 8400
                                                                               19. 3
                                                                                               20. 11
                           17. 190
                         22. (a) 11C_4 (b) 6C_2 \times 5C_2 (c) 6C_4 + 5C_4
23. (i) 14C<sub>9</sub> (ii) 14C<sub>11</sub>
                                                      24. 2(20C_5 \times 20C_6)
25. (i) 21, (ii) 441 (iii) 91
                                                       26. A
                                                                                27. B
                                                       30. C
28. C
                           29. B
                                                                               31. A
32. B
                           33. D
                                                       34. B
                                                                               35. C
                                                       38. C
36. D
                           37. A
                                                                               39. B
                                                       42. 0
40. B
                           41. n = 7
                                                                               43. n^r
44. 1,51,200
                           45. 80
                                                       46. 5<sup>6</sup>
                                                                               47. 18
48. 35
                           49. 7800
                                                       50. 64
                                                                               51. False
52. False
                           53. False
                                                       54. True
                                                                               55. True
56. True
                           57. True
                                                       58. False
                                                                               59. False
60. (a) \leftrightarrow (ii)
                           (b) \leftrightarrow (iii) and
                                                       (c) \leftrightarrow (i)
61. (a) \leftrightarrow (iii)
                           (b) \leftrightarrow (i)
                                                       (c) \leftrightarrow (iv),
                                                                                (d) \leftrightarrow (ii)
62. (a) \leftrightarrow (iv)
                           (b) \leftrightarrow (iii)
                                                      (c) \leftrightarrow (ii),
                                                                                (d) \leftrightarrow (i)
63. (a) \leftrightarrow (i)
                           (b) \leftrightarrow (iii)
                                                       (c) \leftrightarrow (iv),
                                                                                (d) \leftrightarrow (ii)
64. (a) \leftrightarrow (iii)
                           (b) \leftrightarrow (i)
                                                       (c) \leftrightarrow (ii)
```

 $^{15}C_{10} \frac{1}{6}^{5}$  2.  $k = \pm 3$  3. -19

18/04/18

**4.**  $-3003(3^{10})(2^5)$ 

**5.** (i) 
$$-252$$
 (ii)  $\frac{189}{8}x^{17}$ ;  $\frac{-21}{16}x^{19}$  **6.**  $-252$  **7.**  $-1365$  **8.**  $252y^{\frac{5}{2}}x^{\frac{5}{3}}$ 

**6.** 
$$-252$$
 **7.**  $-1365$  **8.**  $252y^{\frac{5}{2}}x^{\frac{5}{3}}$ 

9. 
$$r = 6$$

12. 
$$p = \pm 2$$
 14.  $n = 9$ 

14. 
$$n = 9$$

17. 
$$\frac{17}{54}$$

**25.** 
$${}^{30}C_{15}$$
 **26.**  $\frac{(n+1)(n+2)}{2}$  **27.**  ${}^{16}C_8$  **28.**  $n=12$ 

27. 
$$^{16}C_8$$

**28.** 
$$n = 12$$

**29.** 
$$\frac{1120}{27}a^{-6}a^4$$
 **30.**  $^{28}$  C<sub>14</sub>  $a^{56}$   $b^{14}$  **31.** 1

**30.** 
$$^{28}$$
 C<sub>14</sub>  $a^{56}$   $b^{14}$ 

7. 
$$\frac{15}{8}$$
 cm

7. 
$$\frac{13}{8}$$
 cm

**11.** (i) 
$$4n^3 + 9n^2 + 6n$$
 (ii) 4960  
**18.** C **19.** A

12. 
$$T_r = 6r - 1$$
 17. D  
20. B 21. C

27. 
$$\frac{a}{b}or\frac{b}{c}$$

$$\leftrightarrow$$
 (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii)

**36.** (a) 
$$\leftrightarrow$$
 (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii)(d)  $\leftrightarrow$  (iv)

**1.** 
$$x + y + 1 = 0$$
 **2.**  $x - 4y + 3 = 0$  **3.**  $60^{\circ}$  or  $120^{\circ}$ 

$$2. \ x - 4y + 3 = 0$$

4. 
$$x + y = 7 \text{ or } \frac{x}{6} + \frac{y}{8} = 1$$

7. 
$$y - \sqrt{3}x - 2 + \sqrt{3} = 0$$

8. 
$$3x + 4y + 3 = 0$$

9. 
$$a = \frac{-8}{3}, b = 4$$

$$10. 8x - 5y + 60 = 0$$

11. 
$$\sqrt{3}x + y = 8$$

**12.** 
$$x - 7y - 12 = 0$$

13. 
$$\sqrt{\frac{2}{3}}$$

17. 
$$9x - 20y + 96 = 0$$

**18.** 
$$3x - 4y + 6 = 0$$
 and  $4x - 3y + 1 = 0$ 

**20.** 
$$(0, 2 + \frac{5\sqrt{3}}{2})$$

$$\frac{13}{2}$$
  $x + y + 1 = 0$ 

**44.** 
$$3x - y - 7 = 0$$
,  $x + 3y - 9 = 0$ 

**43.** 
$$x + y + 1 = 0$$

**45.** opposite sides **46.** 
$$13(x^2 + y^2) - 83x + 64y + 182 = 0$$

**47.** 4 
$$x^2$$
  $y^2 = p^2$  ( $x^2 + y^2$ )

**57.** (a) 
$$\leftrightarrow$$
 (iii)

(b) 
$$\leftrightarrow$$
 (i) and

$$(c) \leftrightarrow (ii)$$

**58.** (a) 
$$\leftrightarrow$$
 (iv)

(b) 
$$\leftrightarrow$$
 (iii)

$$(c) \ \leftrightarrow (i),$$

$$(d) \leftrightarrow (ii)$$

**59.** (a) 
$$\leftrightarrow$$
 (iii)

(b) 
$$\leftrightarrow$$
 (i)

(c) 
$$\leftrightarrow$$
 (iv),

$$(d) \leftrightarrow (ii)$$

1. 
$$x^2 + y^2 - 2ax - 2ay + a^2 = 0$$

3. 
$$\frac{a}{2}, \frac{b}{2}$$

$$4. \quad x^2 + y^2 - 2x - 4y + 1 = 0$$

5. 
$$\frac{3}{4}$$

**6.** 
$$x^2 + y^2 + 4x + 4y + 4 = 0$$

$$8. \quad x^2 + y^2 - 2x + 4y - 20 = 0$$

**10.** 
$$x^2 + y^2 - 6x + 12y - 15 = 0$$

11. 
$$\frac{\sqrt{3}}{2}$$

12. ecentricity = 
$$\frac{4}{5}$$
 and foci (4, 0) and (-4, 0)

13.  $\frac{39}{4}$ 

14.  $\frac{4x^2}{81} + \frac{4y^2}{45} = 1$ 

15. 18

16. (2, 4), (2, -4)

17.  $\frac{4a\cos\theta}{\sin^2\theta}$ 

18.  $x^2 + 8y = 32$ 

19.  $m = 1$ 

20.  $x^2 - y^2 = 32$ 

21.  $\frac{\sqrt{13}}{2}$ 

22.  $\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$ 

23.  $x^2 + y^2 - 2x + 2y = 47$ 

13. 
$$\frac{39}{4}$$

**14.** 
$$\frac{4x^2}{81} + \frac{4y^2}{45} = 1$$
 **15.** 18

17. 
$$\frac{4a\cos\theta}{\sin^2\theta}$$

**18.** 
$$x^2 + 8y = 32$$

**19.** 
$$m = 1$$

**20.** 
$$x^2 - y^2 = 32$$

21. 
$$\frac{\sqrt{13}}{2}$$

22. 
$$\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$$

21. 
$$\frac{\sqrt{13}}{2}$$
 22.  $\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$  23.  $x^2 + y^2 - 2x + 2y = 47$ 

24. 
$$x^2 + y^2 - 4x - 10y + 25 = 0$$

**25.** 
$$(x-3)^2 + (y+1)^2 = 38$$

**26.** 
$$x^2 + y^2 - 18x - 16y + 120 = 0$$

**24.** 
$$x^2 + y^2 - 4x - 10y + 25 = 0$$
 **25.**  $(x - 3)^2 + (y + 1)^2 = 38$  **26.**  $x^2 + y^2 - 18x - 16y + 120 = 0$  **27.**  $x^2 + y^2 - 8x - 6y + 16 = 0$ 

20. 
$$x + y = 16x = 10y + 120 =$$

**28.** (a) 
$$y^2 = 12x - 36$$
, (b)  $x^2 = 32 - 8y$ , (c) $4x^2 + 4xy + y^2 + 4x + 32y + 16 = 0$ 

**29.** 
$$3x^2 + 4y^2 - 36x = 0$$

$$30. 9x^2 + 5y^2 = 180$$

**32.** (a) 
$$15x^2 - y^2 = 15$$
 (b)  $9x^2 - 7y^2 + 343 = 0$ , (c)  $y^2 - x^2 = 5$ 

$$43 = 0$$
, (c)  $y^2$ 

**41.** 
$$(x-3)^2 + (y+4)^2 = \frac{45}{13}^2$$

**42.** 
$$x^2 + y^2 - 46x + 22y = 0$$

**43.** 
$$6+2\sqrt{5}$$
,  $2\sqrt{5}$ 

**44.** 
$$\frac{4x^2}{1} + \frac{4y^2}{5} = 1$$

**45.** 
$$4x^2 + 4xy + y^2 + 4x + 32y + 16 = 0$$
 **46.**  $\frac{y^2}{36} - \frac{x^2}{64} = 1$  and  $(0, \pm 10)$ .

46. 
$$\frac{y^2}{36} - \frac{x^2}{64} = 1$$
 and  $(0, \pm 10)$ .

 51. A
 52. B
 53. A
 54. A

 55. D
 56. B
 57. C
 58. A

**59.** A

## 12.3 EXERCISE

2. (i) 1<sup>st</sup> octant (ii) 4<sup>th</sup> octant (iii) viii<sup>th</sup> octant (iv) v<sup>th</sup> octant (v) 2<sup>nd</sup> octant (vi) 3<sup>rd</sup> octant (vii) viii<sup>th</sup> octant (viii) viih octant

- **3.** (i) (3,0,0), (0,4,0), (0,0,2) (ii) (-5,0,0), (0,3,0), (0,0,7) (iii) (4,0,0), (0,-3,0), (0,0,5)
- **4.** (i) (3,4,0), (0,4,5), (3,0,5) (ii) (-5, 3, 0),(0,3,7), (-5, 0, 7) (iii) (4,-3, 0), (0,-3,-5), (4, 0, -5)
- **5.** 5 **6.** 11 **9.** (2,-4, 16) **11.** (-2, -2, -1)
- **12.** (1, 1, -2) **13.** (-3, 4, -7), (7, 2, 5) and (-3, 12, 17) **14.** (4, 7, 6)
- **15.** (4, -5, 1), (3, -2, -1) **16.** a = -2, b = -8, c = 2
- 17.  $\frac{1}{2}, \frac{1}{2}, 9$  18. 2:1 externally
- **19.** vertices are (3,4,5), (-1,6,-7), (1,2,3) and centroid is  $(1,4,\frac{1}{3})$
- **20.** 1:3 externally
- **21.** (2,0,0), (2,2,0), (0,2,0), (0,2,2) (0,0,2) (2,0,2), (0,0,0), (2,2,2)
- 22. A 23. B 24. A 25. B
- **26.** A **27.** B **28.** B **29.** A
- **30.** A **31.** B **32.** A **33.** D
- 34. A 35. Three coordinates planes 36. Three pairs
- **37.** given point **38.** Eight **39.** (0, y, z) **40.** x = 0
- **41.** (0, 0, z) **42.** x = 0, y = 0 **43.** z- coordinates
- **44.** (y, z coordinates) **45.** yz-plane **46.** x-axis **47.**  $\sqrt{333}$
- **48.** a = 5 or -3 **49.** (1, 1, -2)
- **50.** (a)  $\leftrightarrow$  (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (vi) (e)  $\leftrightarrow$  (iv) (f)  $\leftrightarrow$  (v) (g)  $\leftrightarrow$  (viii) (h)  $\leftrightarrow$  (vii) (i)  $\leftrightarrow$  (x) (j)  $\leftrightarrow$  (ix)

3. 
$$\frac{1}{\sqrt[2]{x}}$$

4. 
$$\frac{1}{3}2^{\frac{-2}{3}}$$

6. 
$$\frac{5}{2}(a+2)^{\frac{3}{2}}$$

9. 
$$\frac{8}{5}$$

12. 
$$\frac{1}{15}$$

13. 
$$\frac{7}{2}$$

**14.** 
$$n = 5$$

15. 
$$\frac{3}{7}$$

16. 
$$\frac{1}{4}$$

19. 
$$\frac{m^2}{n^2}$$

**21.** 
$$\sqrt{2}$$

24. 
$$2\sqrt{a}\cos a$$

**26.** 
$$\frac{1}{4\sqrt{2}}$$

**28.** 
$$k = \frac{3}{8}$$

**29.** 
$$3x^2 + 2x + 1 - \frac{1}{x^2}$$

**30.** 
$$3x^2 - \frac{3}{x^2} - \frac{3}{x^4} + 3$$

31. 
$$3x \sec^2 x + 5\sec^2 x + 3\tan x + 3$$

32. 
$$2 \tan x \sec^2 x$$

33. 
$$\frac{55 - 40x - 15x^2}{\left(5x^2 - 7x + 9\right)^2}$$

34. 
$$\frac{-x^5 \cos x + 5 \sec^4 \sin x + 1}{\sin^2 x}$$

$$35. \quad \frac{x}{\sqrt{2}} \csc x \left(2 - x \cot x\right)$$

**36.** 
$$(ax^2 + \cot x)(-q\sin x) + (p+q\cos x)(2ax - \cos ec^2x)$$

37. 
$$\frac{bc\cos x + ad\sin x + db}{\left(c + d\cos x\right)^2}$$

38. 
$$2\cos 2x$$

39. 
$$(2x-7)(30x-43)(3x+5)^2$$

**40.** 
$$x^2 \cos x + 2x \sin x - 2 \sin 2x$$

41. 
$$\frac{3}{4}\sin^2 2x\cos 2x$$

42. 
$$\frac{-(2ax+b)}{(ax^2+bx+c)^2}$$

43. 
$$-2x\sin(x^2+1)$$

44. 
$$\frac{ad-bc}{(cx+d)^2}$$

**45.** 
$$\frac{2}{3}x^{-\frac{1}{3}}$$

46. 
$$\cos x - x \sin x$$

47. 
$$\sec x(x \tan x + 1)$$

48. 
$$\frac{2\alpha}{\alpha^2 - \beta^2}$$

**52.** 
$$k = 6$$
 **53.**  $c = 1$ 

78. 
$$m = \frac{2\sqrt{3}}{3}$$

- (i) to (v) and (viii) to (x) are statements.
- (i) *p* : Number 7 is prime q: Number 7 is odd
- (iii)p: 100 is divisble by 3
  - q:100 is divisible by 11 r: 100 is divisible by 5
- (ii) p : Chennai is in India
  - q: Chennai is capital of Tamil Nadu
- (iv) p: Chandigarh is capital of Haryana
  - q: Chandigarh is the capital of U.P

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- (v)  $p:\sqrt{7}$  is a rational number (vi) p:0 is less than every positive integer  $q:\sqrt{7}$  is an irrational number q:0 is less than every negative integer
- (vii) p: plants use sunlight for photosynthesis q: plants use water for photosynthesis
  - r: plants use carbondioxide for photosynthesis
- (viii) p: two lines in a plane intersect at one pointq: two lines in a plane are parallel
- (ix) p: a rectangle is a quadrilateralq: a rectangle is a 5- sided polygons.
- 3. (i) Compound statement is true and its component statements are : p: 57 is divisible by 2 and q: 57 is divisible by 3
  - (ii) component statement is true and its component statements are : p: 24 is multiple of 4 and q: 24 is multiple of 6
  - (iii) component statement is false and is component statements arep: All living things have two eyesq: All living things have two legs
  - (iv) component statement is true and its component statements are : p:2 is an number ; q:2 is a prime number
- 4. (i) The number 17 is not prime (ii)  $2 + 7 \neq 6$  (iii) Violet are not blue
  - (iv)  $\sqrt{5}$  is not a rational number (v) 2 is a prime number
  - (vi) There exists a real number which is not an irrational number
  - (vii) Cow has not four legs (viii) A leap year has not 366 days
  - (ix) There exist similar triangles which are not congruent
  - (x) Area of a circle is not same as the perimeter of the circle
- 5. (i)  $p \wedge q$  where p: Rahul passed in Hndi; q: Rahul passed in English
  - (ii)  $p \wedge q$  where p: x is even integer; q: y is even integer
  - (iii)  $p \wedge q \wedge r$  where p:2 is factor of 12; q:3 is factor of 12; r:6 is factor of 12
  - (iv)  $p \lor q$  where p: x is an odd integer; q: x+1 is an odd integer
  - (v)  $p \lor q$  where p : a number is divisible by 2, q : it is divisible by 3
  - (vi)  $p \lor q$  where p : x = 2 is a root of  $3x^2 x 10 = 0$ , q : x = 3 is a root of  $3x^2 x 10 = 0$

- (vii)  $p \lor q$  where p: student can take Hindi as an optional paper and q: student can take English as an optional paper.
- **6.** (i) It is false that all rational numbers are real and complex
  - (ii) It is false that all real numbers are rational or irrational
  - (iii) x = 2 is not a root of the quadratic equation  $x^2 5x + 6 = 0$  or x = 3 is not a root of the quadratic equation  $x^2 5x + 6 = 0$
  - (iv) A triangle has neither 3-sides nor 4-sides
  - (v) 35 is not a prime number and it is not a complex number
  - (vi) It is false that all prime integers are either even or odd
  - (vii) |x| is not equal to x and it not equal to -x
  - (viii) 6 is not divisible by 2 or it is not divisible by 3.
- 7. (i) If the number is odd number then its square is odd number
  - (ii) If you take the dinner then you will get sweet dish
  - (iii) If you will not study then you will fail
  - (iv) If an integer is divisible by 5 then its unit digits are 0 or 5
  - (v) If the number is prime then its square is not prime
  - (vi) If a,b and c are in A.P then 2b = a + c.
- **8.** (i) The unit digit of an integer is zero if and only if it is divisible by 5.
  - (ii) A natural number *n* is odd if and only if it is not divisible by 2.
  - (iii) A triangle is an equilateral triangle if and only if all three sides of triangle are equal.
- 9. (i) If  $x \neq 3$  then  $x \neq y$  or  $y \neq 3$ 
  - (ii) If n is not an integer then it is not a natural number.
  - (iii) If the triangle is not equilateral then all three sides of the triangle are not equal
  - (iv) If xy is not positive integer then either x or y is not negative integer.
  - (v) If natural number n is not divisible by 2 and 3 then n is not divisible by 6.
  - (vi) The weather will not be cold if it does not snow.
- **10.** (i) If the rectangle R is rhombus then it is square.
  - (ii) If tomorrow is Tuesday then today is Monday.
  - (iii) If you must visit Taj Mahal you go to Agra.

- (iv) If the triangle is right angle then sum of squares of two sides of a triangle is equal to the square of third side.
- (v) If the triangle is equilateral then all three anlges of triangle are equal.
- (vi) If 2x = 3y then x:y = 3:2
- (vii) If the opposite angles of a quadrilaterals are supplementary then S is cyclic.
- (viii) If x is neither positive nor negative than x is 0.
- (ix) If the ratio of corresponding sides of two triangles are equal then trianges are similar.
- (i) There exists (ii) For all (iii) There exists (iv) For every (v) For all (vi) 11. There exists (vii) For all (viii) There exists (ix) There exists (x) There exists
- 17.. C
- 18. D
- **19.** B
- **20.** D

- 21. C
- **22.** B
- **24.** B

- 25. C
- 26. A
- 28. B

- 29. A
- **30.** C
- **31.** B
- 32. A

- **33.** C
- **34.** A
- 35. C
- **36.** D
- 37. (i), (ii) and (iv) are statement; (iii) and (v) are not statements.

- 0.32 1.
- 1.25

- $\frac{\left|n_{1}(s_{1})^{2}+n_{2}(s_{2})^{2}+n_{1}n_{2}(\overline{x_{1}}-\overline{x_{2}})^{2}\right|}{(n+n)^{2}}$

8.

- 9. 7
- **10.** 1.38
- 11. Mean = 2.8, SD = 1.12
- **12.** 8.9

5000, 251600 **13.** 

- **14.** Mean = 5.17, SD = 1.53
- 15. Mean = 5.5, Var. = 4.26
- **16.** 0.99

**17.** 7.08

**18.** Mean =  $\frac{239}{40}$ , SD = 2.85

19. Var. = 
$$1.16$$
gm,  $S.D = 1.08$  gm

**19.** Var. = 1.16gm, S.D = 1.08 gm **20.** Mean = 
$$a + \frac{d(n-1)}{2}$$
,

S.D = 
$$d\sqrt{\frac{n^2 - 1}{12}}$$

Hashina is more intelligent and consistent

**23.** Mean = 
$$42.3$$
, Var.  $43.81$ 

#### 16.3 EXERCISE

1. 
$$\frac{1}{72}$$

2. 
$$\frac{2}{3}$$

4. (a) 
$$5^{k-1}$$
 elements (b)  $\frac{5^k - 1}{4}$ 

5. 
$$\frac{4}{9}$$

**6.** 0.93

(b) 0.77 (c) 0.51 (d) 0.57 **9.** (a) 
$$\frac{2}{9}$$
 (b)  $\frac{5}{9}$ 

- 10. (a) $p(\text{John promoted}) = \frac{1}{8}$ ,  $p(\text{Rita promoted}) = \frac{1}{4}$ ,  $p(\text{Aslam promoted}) = \frac{1}{2}$ ,  $p(Gurpreet promoted) = \frac{1}{8}$  (b)  $P(A) = \frac{1}{4}$
- **11.** (a) 0.20
  - (b) 0.17 (c) 0.45 (d) 0.13
- (e) 0.15
- **12.** (a)  $S = \{B_1B_2, B_1W, B_2B_1, B_2W, WB_1, WB_2BW_1, BW_2, W_1B, W_1W_2, W_2B, W_2W_1\}$

(b) 
$$\frac{1}{6}$$
 (c)  $\frac{2}{3}$ 

**13.** (a) 
$$\frac{5}{143}$$
 (b)  $\frac{28}{143}$  (c)  $\frac{40}{143}$ 

**14.** (a) 
$$\frac{2}{143}$$
 (b)  $\frac{2}{143}$  (c)  $\frac{25}{26}$  (d)  $\frac{15}{26}$ 

15. 
$$\frac{7}{13}$$

**16.** (a) 
$$p(A) = .25$$
,  $p(B) = .32$ ,  $p(A \cap B) = .17$  (b)  $p(A \cup B) = .40$  (c) .40 (d) .68

17. (a) 
$$\frac{1}{2}$$
 (b)  $\frac{3}{4}$  (c)  $\frac{3}{26}$  (d)  $\frac{5}{36}$ 

**18.** A **19.** B

22. D 23.

**26.** B **27.** C

**30.** False **31.** False

**39.** 
$$E = \{2,4,6\}$$

**42.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (v) (c)  $\leftrightarrow$  (i) (d)  $\leftrightarrow$  (iii) (e)  $\leftrightarrow$  (ii)

**43.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (iii) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (i)